Beyond the Standard Model

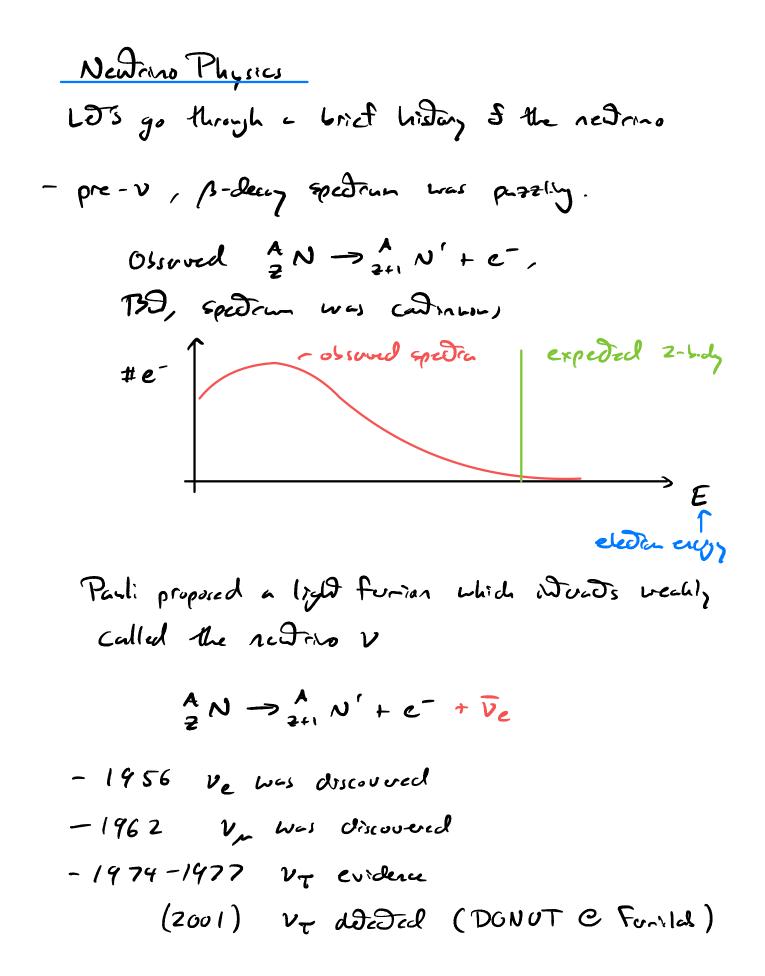
The Minimal Standard Model is extremely successful, & themerical consistent. However, we know it is incomplete from Narious phenomenological and theoretical issues.

Theoretical Issues - No accepted with an with gravity - hiverchy problems, Fine-tuning, A cosmological constant - CP problem

It is gavely accided that the SM is a  
low-may approximation to a more fundanated than,  

$$\mathcal{I} = \mathcal{I}_{SH} + \mathcal{I}_{EH} + \mathcal{S}\mathcal{I}_{BSM}$$
  
Emplet-Hiller Beyond the  
Emplet-Hiller Stadard Hadel  
for classical gravity  
There are may theoretical approaches in looking the  
TSSM physics  
- More deaf.  
- Loss symmetry (GUTS, SUSY,...)  
- More deaf.  
- Loss symmetry (e.g., Landtz Violation)  
- More dimensions  
- Extended fundanetal deaf.  
- ...

Here we will focus on one of the more well-known extensions BSM - NewTrino masses.



Netrinos exilitient parity violdin (Low 1956), one 18t-handled (Gooldbaser 1958), and Z-decays indicate that there are 3 light-families. All consider with SM so for.

Botween 1970 & 1994, may observations of Solar newtrinos indirected a newtrino deficit

4p → <sup>4</sup>He + 2e<sup>+</sup> + 2ve radiu in sur flux predided

Experindally observe Ve-flux ~ 1 (theory predition)

Experiments & SNO (2001) and Super K (1998) found flux (ve + v, ) = theoretical flux. This led to the hypothesis that newtrinos existibility flavor transmutations, i.e., weak eigenstates & propagating states. (cf. CKM matrix & vectoral meson oscillations)

This mixing suggests newtrands have mass!

Let's look at a single Quartur mechanical model, with no spher structure & any Z flavors

(i.e.,  

$$\begin{pmatrix} v_e \\ v_p \end{pmatrix} = \begin{pmatrix} c_1 \cdot \partial - s_1 \partial -$$

Consider a fixed p-state 
$$|Ve > = |Ve(p)\rangle$$
  
A tro,  
 $|Ve(H) > = e^{-iHt}$   
 $= e^{-iHt} (cost(1) - sut(12))$   
 $= e^{-iE_1t} (cost(1) - e^{-iE_2t} sut(2))$ 

Probability to set  $1 \sqrt{2} = t$  is  $P_{e \rightarrow e}(t) = |2 \sqrt{2} | \sqrt{2} |^{2}$   $= |e^{-iE_{1}t} c_{2}^{2} + e^{-iE_{2}t} s_{1}^{2} = (e^{-iE_{1}t} c_{2}^{2} + e^{-iE_{2}t} s_{1}^{2} = (e^{-iE_{1}t} c_{2}^{2} + e^{-iE_{2}t} = 1 - s_{1}^{2} + 2\theta s_{1}^{2} + (E_{1} - E_{1}) + 1/2$ 

In the ultranel Divisitic limit, 
$$|\vec{p}| \gg m_{j} \gg |\vec{p}| \sim E$$
  
 $t \sim L$   
 $E_{j} \approx |\vec{p}| + 1 \frac{m_{j}^{2}}{2 |\vec{p}|}$ 
some distance  $\int_{at time t}^{at time t}$ 

$$\Rightarrow P_{e \to e}(t) = 1 - s L^2 2 \Theta s L^2 \left( \frac{\Delta h_{21}^2 L}{4E} \right)$$

where  $\Delta m_{z_1}^z = m_z^2 - m_1^2$ 

Similar analysis gives  

$$P_{e \rightarrow m}(t) = 5/h^2 \Theta 5/h^2 \left(\frac{\Delta m_{z_1}^2 L}{4E}\right)$$

Notice that we are Not susitive to mi, just Amzi. Bat, experimentally

$$\int \Delta m_{21}^{2} = 9 \times 10^{-3} eV$$

$$\int \Delta m_{32}^{2} = 5 \times 10^{-2} eV$$

Cosmological observation & dired measurematis give My 2 2 eV

The total probability is 1, Perce + Per,= 1 + t. This makes holds in vocume, and assumes colored and monochromedric new prinos (Ithough could estand again to wave puckeds, & also QFT).

Dirac Mass  
Pecall the 
$$\overline{\Psi}_{R}\Psi_{R} = 0 = \overline{\Psi}_{L}\Psi_{L}$$
  
To add a mass term, we need a new field,  
 $\mathcal{L}_{nass}^{D} \sim m_{1}c\phi > \overline{\Psi}_{R}\Psi_{L}$  thic.  
  
Need new d.o.f. to MSM,  $\mathcal{V}_{R}$ .  
 $(1, 1)_{0} \longrightarrow con agree this by array carcedor.$   
No stray  $\mathcal{D}_{S}$ .  
 $(1, 1)_{0} \longrightarrow con agree this by array carcedor.
No stray  $\mathcal{D}_{S}$ .  
 $(1) = 1$  new field  
 $(\mathcal{D}_{T} = \mathcal{J}_{S}\mathcal{D}_{S})$$ 

MSM Yuhawa completings

Side all have 
$$\Delta m^{2}$$
, two possibilities for news spectrum  
 $m^{2}$ 
 $m^{2}$ 

As with the Cleff models, this left nixing  
As with the Cleff models, this left nixing  
Atods biturding with 
$$W^{\pm}$$
,  
 $\overline{L}\mathcal{B}L = (\overline{v}_{L}, \overline{x}_{L})\gamma^{-}\left(\frac{\#}{-\frac{1}{2}i_{5}}W_{L}^{\pm} - \frac{1}{3}\frac{i_{5}}W_{L}^{\pm}}{\frac{1}{2}}\right)\begin{pmatrix} u_{L} \\ x_{L} \end{pmatrix}$   
 $\Rightarrow \overline{L}\mathcal{B}L \supset \overline{v}_{L} (U_{L}^{*})^{+}\left(-\frac{1}{3}i_{5}W_{L}^{\pm}\right)(U_{L}^{*})\hat{k}_{L}$   
 $+ \overline{k}_{L}(U_{L}^{*})^{+}\left(-\frac{1}{3}i_{5}W_{L}^{\pm}\right)(U_{L}^{*})\hat{v}_{L}$   
 $\overline{D}due \qquad U_{PMNS} = (U_{L}^{*})^{+}(U_{L}^{*})$   
Podeconvo - Maki - Nakageve - Salate (PMNS) mixing models  
Mixing angle counting is some as Cleff  
 $\Theta_{12}^{*} = 33.41^{\circ} \frac{10.75^{\circ}}{-0.72^{\circ}}$  Assumes normal ordering  
 $\Theta_{21}^{*} = 49.1^{\circ} \frac{10^{\circ}}{-0.72^{\circ}}$   
 $\overline{S}' = 197^{\circ} \frac{149^{\circ}}{-25^{\circ}}$  (und other of the measure  
Corput with Cleff  $\Theta_{12}^{*}/3^{\circ}, \Theta_{23}^{*} 2^{\circ}, \Theta_{13}^{*} 0.2^{\circ}, S^{*} 70^{\circ}$ 

So, adding neutrino masses "seens" single, take MSM with 19 paranetus, add right-handed rentrinos with 3 mass paranetus + 4 PMNs paranetus. Why is this not accepted as "Ste", and considered as "BSM"? It turns of shee refines are rentral, there is an afterdive way to add raining messes with SM fields.

Majarana Mass Recall for scalar fields, \$\$\$ USarphi arphiLo has conserved Cured La no conserved cured Both are mass toons! For spin-tz, have similar structures · 4 4 € canter cojude 77 US. has conserved Current La no conserved current (Net Copler conj) > Still Law & inverient  $Recall: \Psi^{C} = C \overline{\Psi}^{T}$ 

₹4<sup>c</sup> = ∓C∓<sup>T</sup> ore called <u>Mijorman</u> mass tens.

Propose new rais terns

$$\mathcal{L}_{ress}^{H} \sim () \overline{\nu}_{L} \nu_{L}^{C} = () \overline{\nu}_{L} C \overline{\nu}_{L}^{T}$$

$$Ssre \phi \text{ fidd reduction}$$

Let try verious contrictions  

$$- d=3 \quad \text{tens}$$

$$\overline{V}_{L} \subset \overline{V}_{L}^{T} , \quad \overline{L} \subset \overline{L}^{T}$$

$$\text{hyperdage } Y = +3 \quad +1 \quad +1 \quad +1 \quad \Rightarrow \quad Y \neq 0 \quad \times$$

$$- d=4 \quad \text{tens} , \text{need one Higgs daklet}$$

$$\Rightarrow \quad \text{shill 1 enceonderd SU(2) index }$$

$$(\overline{L} \varphi) \subset \overline{L}^{T} , \quad (\overline{L} \varphi^{C}) \subset \overline{L}^{T} \quad \times$$

$$\int_{N^{0}} \int_{N^{0}} \int_{N^{$$

After SSB, 
$$\Phi^{c} = \frac{g}{J_{z}} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$
  
 $\Rightarrow \int (\overline{L}\Phi^{c}) C(\Phi^{cT}\overline{L}^{T}) + h.c.$   
 $M = \frac{1}{\overline{V}_{L}} \frac{1}{\overline{J}_{z}}$   
 $= \frac{a^{2}}{\overline{J}_{z}} \overline{V}_{L} C \overline{V}_{L}^{T} + h.c.$   
 $= \frac{a^{2}}{\overline{Z}} \overline{V}_{L} C \overline{V}_{L}^{T} + h.c.$   
Majorne mass ten!  
Nother no mass ton generical for  $L$ - leptons.  
Suppose  $M \sim 10^{16}$  GeV (GUT scale)

$$\Rightarrow m_{V} \sim (\frac{246 \text{ GeV}}{10^{16} \text{ GeV}}^{2} \simeq 3 \times 10^{-3} \text{ eV}^{1}$$

$$S_{0}, 2_{mass}^{M} = -1(\bar{L}\phi^{c})C(\bar{L}\phi^{c})^{T} + h.c.$$

Note also that lepton # is not conserved !

$$V_{L} \rightarrow e^{iQ_{L}} v_{L}$$

$$\overline{v}_{L} \rightarrow e^{-iQ_{L}} \overline{v}_{L}$$

To include mixing, 
$$\frac{1}{M} \Rightarrow \left(\frac{1}{M}\right)_{AB} = H_{AB}$$
 [H] = GeV<sup>T</sup>  
Lo finily index  
Consider  $\overline{\nu}_{L}^{A} \subset \overline{\nu}_{L}^{BT} = \left(\overline{\nu}_{L}^{A} \subset \overline{\nu}_{L}^{DT}\right)^{T}$  from space  
 $= -\overline{\nu}_{L}^{B} \subset \overline{\nu}_{L}^{AT}$ ,  $C^{T} = -C$   
 $= \overline{\nu}_{L}^{B} \subset \overline{\nu}_{L}^{AT} \Rightarrow Symmetric !$   
So,  $\mathcal{L}_{mus}^{M} \sim H_{AB} \overline{\nu}_{L}^{A} \subset \overline{\nu}_{L}^{BT}$ 

=> HAD is symptric! HT= H (while Yuhawa in HSM)

$$[\nabla^{P} \nabla^{P} V] + A^{P} Herrite!$$

$$Diagon Jite, \quad U + U^{T} = diagon J$$

$$L = H + H^{T} \Rightarrow J = J^{+} + Herritian$$

$$So, \quad V^{+} J \vee = diagon J, \quad Acal eigenvalues$$

$$L = V^{+} + V, \quad A^{T} = V^{T} + T^{T} \vee = A \quad suce + T^{-} + H$$

$$So, \quad A^{+} A = V^{+} + H^{+} \vee^{*} \vee^{T} + V$$

$$(V \vee^{+})^{*} = 1$$

$$= V^{+} + H^{+} + V \quad diagon J, \quad X \text{ real}$$

$$L = X + iY, \quad X, Y \quad \text{real individual} (X^{T} = X, Y^{T} = Y)$$

$$A^{+}A = \chi^{2} - \chi^{2} + \chi^{T}; \chi - \chi \gamma^{T} \chi$$
$$= \chi^{2} - \chi^{2} + \chi[\chi, \chi]$$

Since AtA is real => [X,Y]=0 => X,Y simultaneously diagon Jizdele WXWT dragen WYWT dragen

$$(HU)^{T} = WV^{T}HVW^{T}$$

$$1 \qquad A$$

$$U = WV^{T}$$

$$= WAW^{T}$$

$$= W(x + iY)W^{T}$$

$$= \vartheta i g$$

So, can diagondière to get mass terms. Dôthe  $\overline{V}_{L} = \overline{V}_{L} (U_{L}^{M})$ , attus as before  $\sum Notice, doined with \overline{V}$ !

$$T\mathcal{P}L = (\overline{v}_{L}, \overline{\ell}_{L}) \gamma^{*} \left( \frac{\#}{-\frac{1}{52}igW_{L}^{-1}} - \frac{1}{52}igW_{L}^{-1}}{\frac{1}{52}igW_{L}^{-1}} \right) \left( \frac{v_{L}}{\ell_{L}} \right)$$

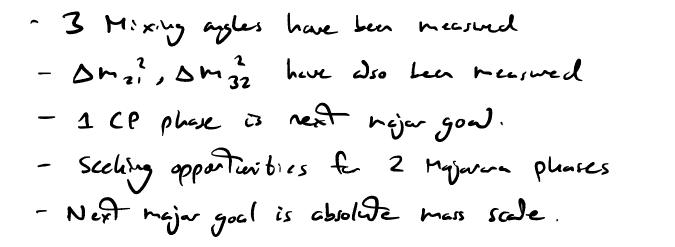
= 
$$\partial_{i_{cy}} \rightarrow terms$$
  
 $-\frac{1}{52} ig \tilde{V}_{L}(U_{L}^{*})\gamma^{*}W_{r}^{+}(U_{L}^{*})\hat{\ell}_{L}$   
 $-\frac{1}{52} ig \tilde{\ell}_{L}(U_{L}^{*})^{\dagger}\gamma^{*}W_{r}^{-}(U_{L}^{*})\hat{V}_{L}$ 

Define 
$$U_n = (U_L^n)(U_L^n)$$
  
 $U_n^+ = (U_L^n)^+ (U_L^n)^+ = U_{pmns}$ 

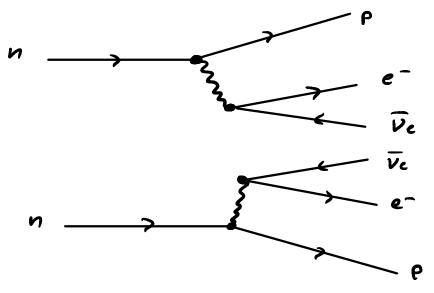
Parameter counting for UPHNS. Since  $U = O_{prives}^{(1)}$  is initial,  $U^+ U = 1$ ⇒ U=e<sup>iGe</sup>,G=G<sup>†</sup> # parans Take G = X + iY, so  $G^{\dagger} = G \implies X = X^{T}$  $Y = -Y^{T}$ とい(い+1) シャ(ハ-1) So,  $U_x = e^{ix\epsilon} \simeq e^{i\epsilon} \Rightarrow \frac{1}{2}n(n+1)$  phases  $U_y = e^{-\gamma\epsilon} = \sin\epsilon (-\sin\epsilon) \Rightarrow \frac{1}{2}n(n-1)$  with y angles For a Dirac mass term, 3 phases Zabort in E (v) 3 phases Jabort in E (v)  $\exists 13(3+1) - 6 + 1 = 1$  phase I a meastrated place For Majorana mass tom. any 3 phases can be absorbed and a

 $\Rightarrow \frac{1}{2}3(3+1) - 3 = 3 \text{ phases}$ 

Car write		
$O_{PnNS} = O_{PNNS} \begin{pmatrix} e^{ix} & 0 \\ 0 & 1 \end{pmatrix}$		
d, pour CP violity phases > so for unconstrained!		
Surray & NeJano mass approaches		
	Divac	Majarana
82	$G(T\phi^{c})v_{p}+h.c.$	$\frac{1}{M}(T\Phi^{c})C(T\Phi^{c})^{T}+h.c.$
New D.O.F.	3	0
Coupling	G., [G]=0	$\frac{1}{M}, \begin{bmatrix} 1\\ M \end{bmatrix} = GeV^{-1}$
Mass Din	4	5
Total Lepton Number	Consovel	Not conserved
Peranders	3 masses	3 masses
	3 mixing ages	3 Mixing angles
	1 SP phase	3 SP chases

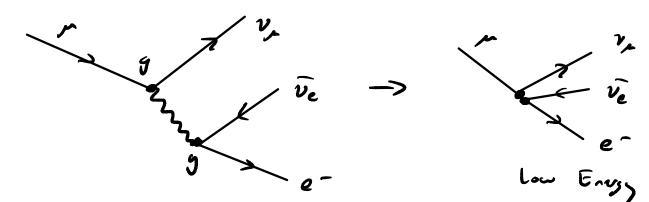


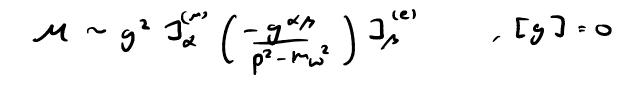
One opportunity is in double producing. It has been observed that  $2n \rightarrow 2p + 2e^- + 2\overline{\nu}_c$ 



See Saw Mechanish

The Majorne mass tern susseds this is a effedive Advedim, e.g., Four-Furni theory from SM



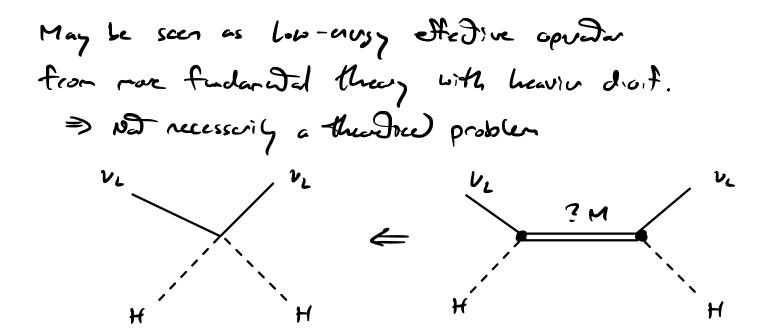


$$if p^{2} (m \omega) \Rightarrow \frac{1}{p^{2} - m \omega^{2}} = \frac{1}{m \omega^{2}} + O(p^{2} - m \omega^{2})$$

This effective theory breaks down I p2~~~

Applying this idea to Majorne new Trinos,  

$$\left(\frac{1}{M}\right)_{AB} \left(\overline{L}_{A} \varphi^{c}\right) C \left(\overline{L}_{B} \varphi^{c}\right)^{T}$$



Thuse are various models which explore this. are common  
are is the Secsaw mechanism. Consider a single  
family,  

$$51_{\text{mism}} = -G(\overline{\Box} \phi^{c}) \upsilon_{R} - \frac{1}{2} M \overline{\upsilon}_{R}^{c} \upsilon_{R} + \text{h.c.}$$
  
 $f_{\text{mism}} = -G(\overline{\Box} \phi^{c}) \upsilon_{R} - \frac{1}{2} M \overline{\upsilon}_{R}^{c} \upsilon_{R} + \text{h.c.}$   
 $f_{\text{mism}} = -\frac{1}{2} (\overline{\upsilon}_{L}, \overline{\upsilon}_{R}^{c}) ( \overset{o}{}_{m} M ) ( \overset{u}{\upsilon}_{R} ) + \cdots$ 

Consider 
$$U = \begin{pmatrix} 1 & m/m \\ -m/m & 1 \end{pmatrix}$$
,  $U U^{T} = U U^{T} = \mathbf{1}$   
For  $M \gg m$ ,  
 $SL = \underbrace{1}_{2} (\overline{v_{L}}, \overline{v_{R}}^{c}) U U^{T} \begin{pmatrix} 0 & n \\ n & m \end{pmatrix} U U^{T} \begin{pmatrix} v_{L}^{c} \\ v_{R} \end{pmatrix}$   
 $= \begin{pmatrix} -m & m & 0 \\ m & 0 \end{pmatrix} + hylor and v$   
 $O = M \end{pmatrix} + hylor and v$   
 $Sy U^{T} \begin{pmatrix} v_{L}^{c} \\ v_{R} \end{pmatrix} = \begin{pmatrix} 1 & -m/m \\ +m/m & 1 \end{pmatrix} \begin{pmatrix} v_{L}^{c} \\ v_{R} \end{pmatrix}$   
 $= \begin{pmatrix} v_{L}^{c} - m & v_{R} \\ v_{R} + m & v_{L}^{c} \end{pmatrix}$