Feynman Rules - Self-Interacting Complex Scalar theory

The Lagrangian density for a self-interacting complex-scalar field theory is given by

$$\mathcal{L} = \partial_{\mu}\varphi^{\dagger} \partial^{\mu}\varphi - m^{2}\varphi^{\dagger}\varphi - \lambda(\varphi^{\dagger}\varphi)^{2}$$

where m is the mass parameter and λ is the coupling.

Feynman Rules

Here we give the Feynman rules for the scattering amplitude \mathcal{M} ,

 $i\mathcal{M} = \text{sum of all connected, amputated diagrams},$

where the diagrams are evaluated according to the following rules:

- Draw all topologically distinct diagrams at a given order;
- For each internal scalar line, attach a propagator

$$\xrightarrow{p} = \frac{i}{p^2 - m^2 + i\epsilon};$$

• For each vertex, assign



• For each external line, place the particle on the mass-shell $p^2 = m^2$ and attach a wavefunction factor



- Impose momentum conservation at each vertex;
- For each internal loop momentum k not fixed by momentum conservation, integrate $\int \frac{\mathrm{d}^4 k}{(2\pi)^4}$;
- Multiply the contribution for each diagram by an appropriate symmetry factor \mathcal{S}^{-1} .