## Feynman Rules - Self-Interacting Scalar theory

The Lagrangian density for a self-interacting real-scalar field theory is given by

$$\mathcal{L} = \frac{1}{2} \partial_{\mu} \varphi \partial^{\mu} \varphi - \frac{1}{2} m^2 \varphi^2 - \frac{1}{4!} \lambda \varphi^4$$

where m is the mass parameter and  $\lambda$  is the quartic coupling.

## Feynman Rules

Here we give the Feynman rules for the scattering amplitude  $\mathcal{M}$ ,

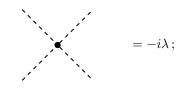
 $i\mathcal{M} =$ sum of all connected, amputated diagrams,

where the diagrams are evaluated according to the following rules:

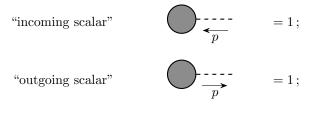
- Draw all topologically distinct diagrams at a given order;
- For each internal scalar line, attach a propagator

$$\xrightarrow{p} = \frac{i}{p^2 - m^2 + i\epsilon};$$

• For each vertex, assign



• For each external line, place the particle on the mass-shell  $p^2 = m^2$  and attach a wavefunction factor



- Impose momentum conservation at each vertex;
- For each internal loop momentum k not fixed by momentum conservation, integrate  $\int \frac{\mathrm{d}^4 k}{(2\pi)^4}$ ;
- Multiply the contribution for each diagram by an appropriate symmetry factor  $\mathcal{S}^{-1}$ .